

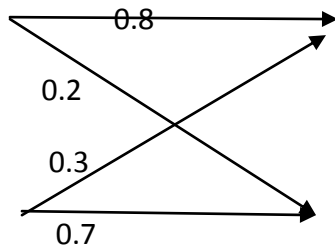
Department of ELECTRONICS & COMMUNICATION ENGG.

Numerical Question Bank

DIGITAL COMMUNICATION (EC-503) Semester: 5TH

INSTRUCTIONS. 1. All questions with their solution are submitted till 27 October 2014.

Question-1 Find the mutual information and channel capacity of the channel shown in figure below. Given $P(X1) = 0.6$ and $P(X2) = 0.4$.



Question-2 A random variable has an exponential PDF given by $f(x) = ae^{(-b|x|)}$ where a and b are constant find (a) the relation between a and b. (b) the distribution function of x.

Question3- Apply Shannon Fano Coding Procedure to find coding efficiency for the following message ensemble. [Take $M = 2$]

$[X] = [x1, x2, x3, x4, x5, x6, x7]$

$[P] = [0.4, 0.2, 0.12, 0.08, 0.08, 0.08, \text{ and } 0.4]$

Question-4 an urn contains 4 white and 3 black balls. Two balls are drawn successively with Denoting the number of black balls:

- Find the probability function of X.
- Draw the chart and histogram

Question-4 A fair die is tossed 5 times. A toss is called a success if face 1 or 6 appears, find:

- The probability of 2 successes.
- The mean and standard deviation for the number of successes.

Question-5 An signal is expressed by the equation $x(t) = 3\cos(50 \pi t) + 10\sin(300 \pi t) - \cos(100 \pi t)$. Calculate the nyquist rate for this signal.

Question-6 Find the nyquist rate and nyquist interval for the signal $x(t) = 1/2 \pi \cos(4000 \pi t) \cos(1000 \pi t)$.

Question-7 A quaternary source generates information with probabilities $P_1 = 0.2$, $P_2 = 0.3$, and $P_4 = 0.4$. Find the entropy of the system. What percentage of maximum possible information is being generated by this source?

Question-8 An event has six possible outcomes with the probabilities $P_1 = 1/2$, $p_2 = 1/4$, $p_3 = 1/8$, $P_4 = 1/16$, $P_5 = 1/32$, $P_6 = 1/32$. Find the entropy of the system. Also the rate of information if there are 16 outcomes per second.

Question-9 A continuous signal is band limited to 5Khz. The signal is quantized in 8 levels of a PCM system with the probabilities 0.25, 0.2, 0.2, 0.1, 0.1, 0.05, 0.05 and 0.05. Calculate the entropy and the rate of information.

Question-10 Two sources are generating as given below.

Source-1 $P_1 = 1/4$, $P_2 = 1/4$, $P_3 = 1/4$, $P_4 = 1/4$

Source-2 $P_1 = 1/2$, $P_2 = 1/4$, $P_3 = 1/8$, $P_4 = 1/8$

The message rates are respectively 200 and 250 messages per second. Compare H and R of sources.

Question-11 An urn contains 3 white and 4 black balls. Two balls are drawn successively with Denoting the number of white balls: Find the probability function of X .

Question-12 24 telephone channels, each band limited to 3.4 KHz, are to be time division multiplexed by using PCM. Calculate the bandwidth of PCM System for 128 quantization levels and an 8 KHz sampling frequency.

Question-13 A container contains 3 white and 4 black balls. Two balls are drawn successively with Denoting the number of white balls: Find the discrete function for random variable X .

Question-14 Find the constant C so that the function

$$f(x) = \begin{cases} C(x-1), & 1 < x < 4 \\ 0 & \text{otherwise} \end{cases}$$

Question-15 For the PDF $f(x) = \begin{cases} \left(\frac{b}{a}\right)x + b, & x < 0 \\ \left(-\frac{b}{a}\right) + b & x > 0 \end{cases}$

(a) The relationship between a and b

(b) $P(X > a/2)$

Question-16 Apply Shannon Fano Coding Procedure to find coding efficiency for the following message ensemble. [Take $M = 2$]

$[X] = [x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8]$

[P] = [1/4, 1/8, 1/16, 1/16, 1/16, 1/4, 1/16, 1/8]

Question17-Apply Haffman Coding Procedure to find coding efficiency for the following message ensemble. [Take M = 2]

[X] = [x1, x2, x3, x4, x5, x6, x7]

[P] = [0.4, 0.2, 0.12, 0.08, 0.08, 0.08, and 0.4]

Question18- The generate polynomial of a (7,4) cycle code is $g(x) = 1+x+x^3$. Find the 16 code words of this code.

Question-19 8 channels, each band limited to 2.5 KHz, are to be time division multiplexed by using PCM. Calculate the bandwidth of PCM System for 64 quantization levels and an 4 KHz sampling frequency.

Question-20 Show the relation between Mean, Variance and Standard Deviation.